

**RATIOS AND PROPORTIONS** Guided NotesWhat is a Ratio?

A ratio is a comparison of a number  $a$  and a non-zero number  $b$  using division.

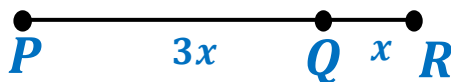
There are three different ways of writing a ratio:

$$\frac{a}{b} \quad a : b \quad a \text{ to } b$$

The ratio is written in simplest form and can be simplified if the quantity in the numerator and denominator is of same units.

$$4\text{ft}:6\text{ft} \quad \Rightarrow \quad \frac{4\text{ft}}{6\text{ft}} \quad \Rightarrow \quad \frac{2\text{ft}}{3\text{ft}} \quad \Rightarrow \quad 2\text{ft}:3\text{ft}$$

**Problem 1:** In the figure below,  $PQ : QR$  is  $3 : 1$ . Find the values of  $PQ$  and  $QR$  if  $PR = 28$ .



Let  $x$  be the length of  $QR$ . Since the ratio of  $PQ$  to  $QR$  is  $3 : 1$ , we can write  $3x : x$ .

$$\Rightarrow \quad 3x + x = 28 \quad \text{By Segment Addition postulate } PQ + QR = PR$$

$$\Rightarrow \quad 4x = 28 \quad \Rightarrow \quad x = 7$$

$$\Rightarrow \quad QR = x = 7$$

$$\Rightarrow \quad PQ = 3x = 3 \times 7 \quad \Rightarrow \quad PQ = 21$$

**RATIOS AND PROPORTIONS** Guided NotesWhat is a Proportion?

A proportion is an equation having two ratios equal.

$$\frac{a}{b} = \frac{c}{d}$$

$$b \ \& \ c \quad \Rightarrow \quad \text{means}$$

$$a \ \& \ d \quad \Rightarrow \quad \text{extremes}$$

Cross-Product Property in Proportions

In a proportion, the product of extremes is equal to the product of means.

$$\frac{a}{b} = \frac{c}{d}$$

$$\Rightarrow \quad ad = bc$$

**Problem 2:** Solve the proportion  $\frac{4}{3} = \frac{y+2}{6}$ .

Apply the cross product property of proportions:

$$\Rightarrow \quad 6 \times 4 = 3 \times (y + 2)$$

$$\Rightarrow \quad 24 = 3y + 6$$

$$\Rightarrow \quad 24 - 6 = 3y \quad \Rightarrow \quad 3y = 18$$

$$\Rightarrow \quad y = 6$$