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## Approximating Square Roots

## Answers:

Part A: Find the value of the following.

1) $\pm \sqrt{36}= \pm 6$
2) $\sqrt{-4}$ undefined
3) $\sqrt{\mathbf{9 0 0}}=\mathbf{3 0}$
4) $\pm \sqrt{\mathbf{1 6 9}}= \pm 13$

Part B: Find two consecutive integers between $\sqrt{46}$ lies.

## Solution:

The radicand is 45 .

The closest perfect square number less than 46 is 36 .

The closest perfect square number greater than 46 is 49.

$$
\begin{aligned}
\sqrt{36} & <\sqrt{46} \\
6 & <\sqrt{49} \\
& <\sqrt{46}<7
\end{aligned}
$$

The square root of $\sqrt{46}$ is between 6 and 7 .
$\qquad$
$\qquad$ Date: $\qquad$

## Approximating Square Roots

Part C: Determine two rational numbers with two decimal places between which $\sqrt{46}$ lies.

## Solution:

Since 45 is between 36 and $49, \sqrt{46}$ must be between $\sqrt{36}$ and $\sqrt{49}$.

$$
\begin{aligned}
\sqrt{36} & <\sqrt{46}<\sqrt{49} \\
6 & <\sqrt{46}<7
\end{aligned}
$$

By estimation, we have:
6. $1^{2}=37.21$
$6.2^{2}=38.44$
$6.3^{2}=39.69$
$6.4^{2}=40.96$
$6.5^{2}=42.25$
$6.6^{2}=43.56$
6. $7^{2}=44.89 \quad$ So, $\sqrt{46}$ lies between 6.7
$6.8^{2}=46.24 \quad$ and 6.8 .

To find the two rational numbers with two decimal places between which $\sqrt{46}$ lies, let's estimate further:
6. $74^{2}=45.4276$
$6.75^{2}=45.5625$
$6.76^{2}=45.6976$
$6.77^{2}=45.8329$
$6.78^{2}=45.9684$ So, $\sqrt{46}$ lies between
$6.79^{2}=46.1041 \quad 6.78$ and 6.79.

The square root of $\sqrt{46}$ is between
6.78 and 6.79.
$\qquad$ Period: $\qquad$ Date: $\qquad$

## Approximating Square Roots

Part D: Approximate $\sqrt{46}$ up to the third estimate by averaging.

## Solution:

Since 46 is between 46 and $49, \sqrt{46}$ must be between $\sqrt{36}$ and $\sqrt{49}$.

$$
\begin{aligned}
\sqrt{36} & <\sqrt{46}<\sqrt{49} \\
6 & <\sqrt{46}<7
\end{aligned}
$$

Step 1: The integer closest to $\sqrt{46}$ is 7 .
The first estimate is 7.

Step 2: Divide the radicand by the first estimate.

$$
46 \div 7 \approx 6.57
$$

Step 3: To find the second estimate, find the average of the quotient in Step 2 and the first estimate.

$$
\frac{6.57+7}{2}=\frac{13.57}{2}=6.785
$$

The second estimate is 6.785 .

Step 4: Repeat Step 2. But this time, divide the radicand by the second estimate.

$$
46 \div 6.785 \approx 6.78
$$

Step 5: To find the third estimate, repeat Step 3. This time, find the average of the quotient in Step 4 and the second estimate.

$$
\frac{6.78+6.785}{2}=\frac{13.565}{2}=6.7825
$$

The closest approximate of $\sqrt{46}$ is 6.7825 .

